

### 22.6.5 MG road-map: Dynamicist on a turntable (ice-skater)

A dynamics instructor stands on a spinning turntable and swings a heavy dumbbell inward and outward to change his spin-rate (similar to the ice-skater).

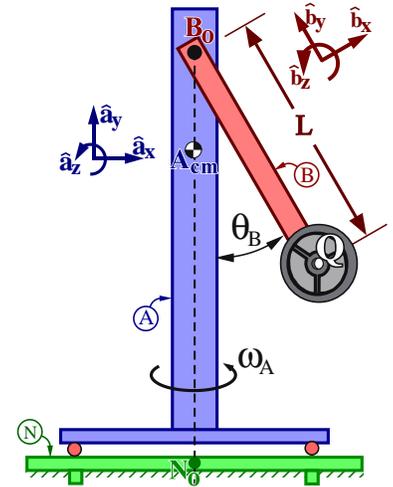
The schematic (below-right) shows a rigid body  $A$  (modeling the instructor's legs, torso, and head) that rotates (without friction) relative to Earth (a Newtonian reference frame  $N$ ) about a vertical axis that is fixed in both  $A$  and  $N$  and which passes through both point  $N_o$  of  $N$  and point  $A_{cm}$  ( $A$ 's center of mass).

A massless rigid arm  $B$  (modeling the instructor's arms and hands) attaches to  $A$  by a revolute motor (shoulder/muscles) whose revolute axis is horizontal and located at point  $B_o$  of  $B$  ( $B_o$  lies on the vertical axis connecting  $N_o$  and  $A_{cm}$ ).

The motor (muscles) **specifies**  $B$ 's angle  $\theta_B$  relative to  $A$  to change in a known (prescribed) manner from 0 to  $\pi$  rad in 4 seconds ( $\theta_B = \pi \frac{t}{4}$ ).

A heavy dumbbell  $Q$  (modeled as a particle) is rigidly attached (welded) to the end of  $B$  (the instructor's hands).

Right-handed orthogonal unit vectors  $\hat{a}_x, \hat{a}_y, \hat{a}_z$  and  $\hat{b}_x, \hat{b}_y, \hat{b}_z$  are fixed in  $A$  and  $B$ , respectively, with  $\hat{a}_y$  vertically-upward,  $\hat{b}_z = \hat{a}_z$  parallel to the revolute motor's axis, and  $\hat{b}_y$  directed from  $Q$  to  $B_o$ .



Quantity	Symbol	Type	Value
Earth's gravitational constant	$g$	Constant	$9.8 \frac{m}{s^2}$
Distance between $Q$ and $B_o$	$L$	Constant	0.7 m
Mass of $Q$	$m$	Constant	12 kg
$A$ 's moment of inertia about line $\overline{A_{cm} B_o}$	$I_{yy}$	Constant	$0.6 \text{ kg m}^2$
Angle from $\hat{a}_y$ to $\hat{b}_y$ with $+\hat{a}_z$ sense	$\theta_B$	<b>Specified</b>	$0.25 \pi t$ rad
$\hat{a}_y$ measure of $A$ 's angular velocity in $N$	$\omega_A$	Variable	

Complete the **MG road-map** for the turntable's "spin-rate"  $\omega_A$  (Note: The "about point" is not unique)

Variable	Translate/ Rotate	Direction (unit vector)	System $S$	FBD of $S$	About point*	<b>MG road-map equation</b>
$\omega_A$				<b>Draw</b>		
$\omega_A$	Dot( <span style="background-color: yellow;"></span> , System( <span style="background-color: yellow;"></span> ), GetDynamics( <span style="background-color: yellow;"></span> ) )					<b>MotionGenesis</b> command ©

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