

16.1 ♣ Two types of forces in a free-body diagram (FBD) (Section 18.6).

From an engineering/FBD perspective, the two types of forces are and .

16.2 ♣ What is 1 Newton and 1 lbf? (Section 21.1).

1 Newton is defined as (circle all that apply)	<input type="checkbox"/> $1 \frac{\text{kg m}}{\text{s}^2}$	<input type="checkbox"/> $9.81 \frac{\text{kg m}}{\text{s}^2}$	<input type="checkbox"/> $32.2 \frac{\text{kg m}}{\text{s}^2}$	<input type="checkbox"/> None of these
1 lbf is defined as or approximately equal to (circle all that apply)	<input type="checkbox"/> $1 \text{ kg} \cdot \frac{\text{m}}{\text{s}^2}$	<input type="checkbox"/> $1 \text{ slug} \cdot \frac{\text{ft}}{\text{s}^2}$	<input type="checkbox"/> $1 \text{ lb}_m \cdot \frac{\text{ft}}{\text{s}^2}$	
	<input type="checkbox"/> $9.81 \text{ kg} \cdot \frac{\text{m}}{\text{s}^2}$	<input type="checkbox"/> $9.81 \text{ slug} \cdot \frac{\text{ft}}{\text{s}^2}$	<input type="checkbox"/> $9.81 \text{ lb}_m \cdot \frac{\text{ft}}{\text{s}^2}$	
	<input type="checkbox"/> $32.2 \text{ kg} \cdot \frac{\text{m}}{\text{s}^2}$	<input type="checkbox"/> $32.2 \text{ slug} \cdot \frac{\text{ft}}{\text{s}^2}$	<input type="checkbox"/> $32.2 \text{ lb}_m \cdot \frac{\text{ft}}{\text{s}^2}$	

Using the exact Section 21.1 NIST conversion factor for lbf to kg and the exact conversion factor $1 \text{ inch} \triangleq 2.54 \text{ cm}$, show how to calculate the conversion factor for lbf to Newton.

Result

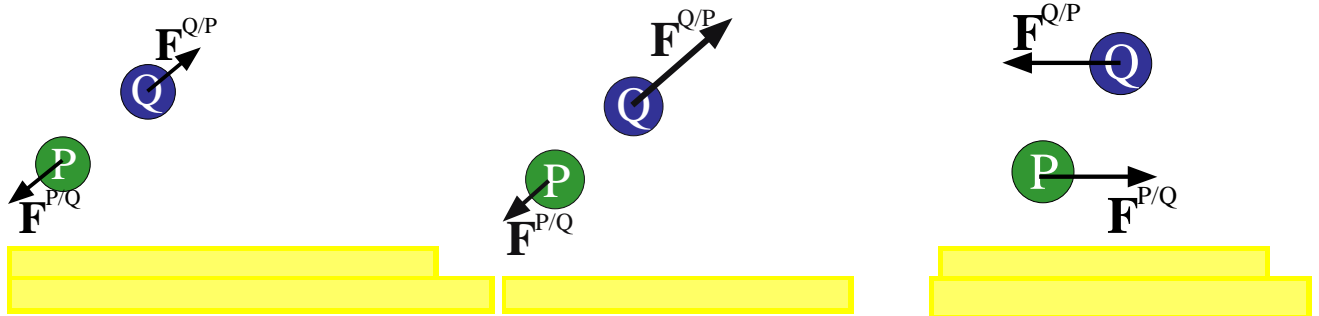
$$1 \text{ lbf} \approx \frac{\text{lbm ft}}{\text{s}^2} * \frac{\text{kg}}{\text{lbm}} * \frac{\text{inch}}{\text{ft}} * \frac{\text{m}}{\text{inch}} * \frac{\text{ft}}{\text{m}} * \frac{\text{N}}{\text{kg m/s}^2} \approx 4.45 \text{ N}$$

16.3 ♣ Force concepts (Section 18.3).

A force is a well-defined quantity:	True/False
The resultant of a set of forces is a force.	True/False
In the SI (metric) system, the units of force are:	<input type="text"/>
In the SI (metric) system, the units of impulse are:	<input type="text"/>
$\vec{F} = m\vec{a}$ is violated if a non-zero forces exists without the presence of a massive object	True/False
$\vec{F} = m\vec{a}$ is violated if mass exists without the presence of force	True/False

16.4 ♣ Law of action/reaction (Section 18.1).

Circle the forces that obey the law of action/reaction. Explain why each pair obeys/disobeys.



16.5 ♣ Coulomb's friction law (Section 21.6).

The range for Coulomb's coefficient of static friction is always $0 \leq \mu_s \leq 1$. True/False.

Coulomb's friction law is exact/accurate (< 1% error)/approximate/completely wrong.

16.6 ♣ Force and mass concepts (Section 21.1).

The center of mass and center of gravity may be different points.	True/False
The center of gravity of a rigid body always exists.	True/False

16.7 ♣ **Convert U.S. units of psi to SI units of Pascals and estimate stress** (Section 21.1).

Use **each** conversion factors (number) below at **least once** (and others you should know) to convert units of 1 inch to **x** meters, 1 lbf (pound-force) to **y** Newtons, and 1 psi ($\frac{\text{lbf}}{\text{inch}^2}$) to **z** Pascals ($\frac{\text{N}}{\text{m}^2}$). Express your results for **z** in terms of the intermediate conversion factors **x** and **y**.

$$1 \text{ inch} \triangleq 2.54 \text{ cm} \qquad 1 \text{ kg} \approx 2.2 \text{ lbm} \qquad 1 \text{ g}_{\text{Earth}} \approx 32.2 \frac{\text{ft}}{\text{s}^2}$$

Conversion Equation (with numbers and units) for calculating result.

1 in = x m	x = 1 in * $\frac{2.54 \text{ cm}}{1 \text{ in}}$ * $\frac{1 \text{ m}}{100 \text{ cm}}$ ≈ 0.0254	Example of how to do units conversions
1 lbf = y N	y = ≈ 4.45	
1 psi = z Pa	z = ≈ 6894.757	Express z in terms of x and y

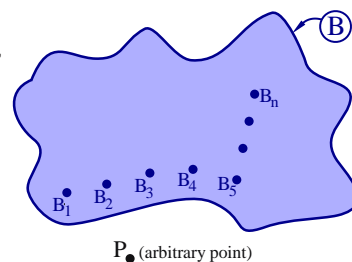
Engineering skill: Estimate/approximate order-of-magnitudes for mass, force, and stress.

Mass of a laptop computer	0.04/0.4/4/40/400 lbm
Weight of a laptop computer	0.04/0.4/4/40/400 lbf
Weight of a laptop computer	0.02/0.2/2/20/200 Newtons
Gage pressure in a bike tire (remember pumping up a bike/car tire?)	0.05/0.5/5/50/500 psi
Gage pressure in a bike tire	0.03/0.3/3/30/300 kPa
Stress of a 200 lbf person on one flat sneaker on a wood floor	0.05/0.5/5/50/500 psi
Stress of a 120 lbf person on one stiletto heel on a wood floor	0.03/0.3/3/30/300 psi

16.8 ♣ **Forces on an aluminum body** (Sections 18.4, 18.2, and 19.4).

Consider 6.022×10^{23} molecules of aluminum (≈ 27 grams) which define a body *B*. The quantities under investigation (and related moments) are:

- \vec{F}^B the resultant of all forces on *B*
- $\vec{F}_{\text{internal}}^B$ the resultant of all internal forces in *B*
- $\vec{F}_{\text{external}}^B$ the resultant of all external forces on *B*
- \vec{F}^{B_1/B_2} the force on molecule *B*₁ from molecule *B*₂



Condition	Static equilibrium?	Circle the following statements that are always true.			
<i>B</i> is rigid	Yes	$\vec{F}^B = \vec{0}$	$\vec{F}_{\text{internal}}^B = \vec{0}$	$\vec{F}_{\text{external}}^B = \vec{0}$	$\vec{F}^{B_1/B_2} = \vec{0}$
		$\vec{M}^{B/P} = \vec{0}$	$\vec{M}_{\text{internal}}^{B/P} = \vec{0}$	$\vec{M}_{\text{external}}^{B/P} = \vec{0}$	$\vec{M}^{\vec{F}^{B_2/B_1}/P} = \vec{0}$
<i>B</i> is flexible (a thin ruler)	Yes	$\vec{F}^B = \vec{0}$	$\vec{F}_{\text{internal}}^B = \vec{0}$	$\vec{F}_{\text{external}}^B = \vec{0}$	$\vec{F}^{B_1/B_2} = \vec{0}$
		$\vec{M}^{B/P} = \vec{0}$	$\vec{M}_{\text{internal}}^{B/P} = \vec{0}$	$\vec{M}_{\text{external}}^{B/P} = \vec{0}$	$\vec{M}^{\vec{F}^{B_2/B_1}/P} = \vec{0}$
<i>B</i> is rigid	No	$\vec{F}^B = \vec{0}$	$\vec{F}_{\text{internal}}^B = \vec{0}$	$\vec{F}_{\text{external}}^B = \vec{0}$	$\vec{F}^{B_1/B_2} = \vec{0}$
		$\vec{M}^{B/P} = \vec{0}$	$\vec{M}_{\text{internal}}^{B/P} = \vec{0}$	$\vec{M}_{\text{external}}^{B/P} = \vec{0}$	$\vec{M}^{\vec{F}^{B_2/B_1}/P} = \vec{0}$
<i>B</i> is molten (liquid metal)	No	$\vec{F}^B = \vec{0}$	$\vec{F}_{\text{internal}}^B = \vec{0}$	$\vec{F}_{\text{external}}^B = \vec{0}$	$\vec{F}^{B_1/B_2} = \vec{0}$
		$\vec{M}^{B/P} = \vec{0}$	$\vec{M}_{\text{internal}}^{B/P} = \vec{0}$	$\vec{M}_{\text{external}}^{B/P} = \vec{0}$	$\vec{M}^{\vec{F}^{B_2/B_1}/P} = \vec{0}$

16.9 ♣ **Measurement accuracies of the Universal Gravitational Constant G** (Section 21.3).

The gravitational force on a particle Q of mass m^Q from a particle P of mass m^P can be written in terms of Q 's position vector from P as

$$\vec{F}^{Q/P} = \frac{-G m^P m^Q}{|\vec{r}^{Q/P}|^3} \vec{r}^{Q/P} \quad (21.3)$$

What are the dimensions of G (in terms of mass, length and time) and the SI units of G ?

Result: Dimensions of G : (in terms of mass, length, time)
 Units of G : (in terms of kg, m, s)

The number of significant digits the first measurement of the “*Universal Gravitational Constant*” G in 1798 by Cavendish and recent (year 2000⁺) experiments of G are estimated to be accurate to:

Experiments in 1798	1	2	5	7	infinite
Experiments in 2000 ⁺	1	2	5	7	infinite

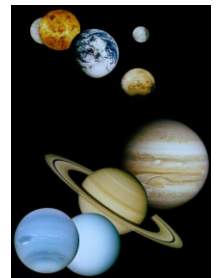
Note: Section 21.3 discusses experiments involving G .

16.10 ♣ **According to Newton’s laws (theories), is the universe static?** (Sections 18.2 and 19.3)

Consider the system S consisting of all matter, life, forces, etc.^a

- Newton’s laws dictates the resultant of all forces on S is $\vec{0}$, i.e., $\vec{F}^S = \vec{0}$. True/False.
- The moment of all forces on S about any point P is $\vec{0}$, i.e., $\vec{M}^{S/P} = \vec{0}$. True/False.
- Newton’s laws dictates the universe is in **static equilibrium**. True/False.
- Newton’s 1st/2nd/3rd law explains my answer? (circle one)

Why:



^a Carbon 12 has $\approx 6.02 \times 10^{23}$ molecules. The universe has $\approx 10^{80}$ molecules.

16.11 ♣ **Free-Body Diagrams for 3D three-balloon system.**

The picture below shows a cup hanging by strings from three motionless helium-filled balloons. Draw **FBDs** of each system for the given assumptions.



Helium is lighter than air.

<u>FBD of cup:</u>	<u>FBD of left string:</u>	<u>FBD of left balloon:</u>
Assumptions in FBD Only relevant forces are Earth’s uniform gravity and contact forces from strings (no wind/air resistance, electromagnetic forces, etc.)	Assumptions in FBD String is inextensible. Only relevant forces are tension in string (gravity/other forces are negligible compared to tension.)	Assumptions in FBD Relevant forces are gravity from Earth, fluid pressure from air (buoyancy), and contact from strings and other balloons.